

## Homework #2 – ECEN 667 Fall 2025

Due September 25, 2025 at 8 AM

**Problem 1.** Consider a two-bus case in which there is a classical synchronous generator at each bus. The transmission line connecting them has  $R = 0.05$ ,  $X = 0.15$ . The generator at Bus 1 has  $H = 2.3$ ,  $X'_d = 0.18$ , and is producing 50 MW with a terminal voltage magnitude of 1.02 per-unit. The generator at bus 2 has  $H = 4.3$ ,  $X'_d = 0.21$ , with a terminal voltage magnitude of 1.04 per-unit, and is the slack (reference) bus.

- Create the case in PowerWorld and solve the power flow to get the voltage phasors and complex powers for each of the two generators.
- Find  $\mathbf{Y}$  and  $\mathbf{Y}_{aug}$  for this system, for the initial conditions given.
- List all the variables and equations for the dynamical system.
- Find the initial conditions of all variables and verify that the system is in steady state.

**Problem 2.** Using PowerWorld with the AGL37\_TS case, change the contingency to a zero impedance, three-phase fault on the line between buses 28 and 31 at the bus 31 end. Assume this fault is cleared by opening the line.

- What is the max fault duration such that the frequency remains below 60.3 Hz?
- What is the max fault duration such that no generator loses synchronism?
- Repeat 2.a and 2.b with a fault midway down the line.

**Problem 3.** Consider a generator, similar to the example discussed in class, except that the terminal voltage of the generator is  $\bar{V}_s = 1.0261 \angle 25.39^\circ$  and it is producing 200 MW and 57.24 Mvar (assuming a 100 MVA base). Assume a GENSAL model is used with parameters  $H=3.0$ ,  $D=0$ ,  $R_a = 0$ ,  $X_d = 2.1$ ,  $X_q = 2.0$ ,  $X'_d = 0.3$ ,  $X''_d = X''_q = 0.2$ ,  $X_l = 0.13$ ,  $T'_{do} = 7.0$ ,  $T''_{do} = 0.07$ ,  $T'''_{qo} = 0.07$ ,  $S(1.0) = 0.02$ , and  $S(1.2) = 0.1$ . Manually calculate the following.

- Saturation function coefficients
- Initial values of all state variables
- Field voltage