

Homework 4 solutions

4.10

From Eq. (4.5.10)

$$L_1 = 2 \times 10^{-7} \ln \left(\frac{D}{r'} \right) \frac{\text{H}}{\text{m}} \quad D = 4 \text{ ft}$$

$$L_1 = 2 \times 10^{-7} \ln \left(\frac{4}{1.6225 \times 10^{-2}} \right) \quad r' = e^{\frac{-1}{2}} \left(\frac{.5}{2} \right) \left(\frac{1 \text{ ft}}{12 \text{ in}} \right)$$

$$L_1 = \underline{1.101 \times 10^{-6}} \frac{\text{H}}{\text{m}} \quad r' = 1.6225 \times 10^{-2} \text{ ft}$$

$$X_1 = \omega L_1 = (2\pi 60)(1.101 \times 10^{-6})(1000) = \underline{0.4153 \Omega / \text{km}}$$

4.11

$$(a) \quad L_1 = 2 \times 10^{-7} \ln \left(\frac{4.8}{1.6225 \times 10^{-2}} \right) = 1.138 \times 10^{-6} \text{ H/m}$$

$$X_1 = \omega L_1 = 2\pi(60)(1.138 \times 10^{-6})(1000) = 0.4292 \Omega / \text{km}$$

$$(b) \quad L_1 = 2 \times 10^{-7} \ln \left(\frac{3.2}{1.6225 \times 10^{-2}} \right) = 1.057 \times 10^{-6} \text{ H/m}$$

$$X_1 = 2\pi(60)(1.057 \times 10^{-6})(1000) = 0.3986 \Omega / \text{km}$$

L_1 and X_1 increase by 3.35% (decrease by 4.02%) as the phase spacing increases by 20% (decreases by 20%).

4.20

$$D_{eq} = \sqrt[3]{10 \times 10 \times 20} = 12.6 \text{ m}$$

$$\text{From Table A.4, } D_s = (0.0435 \text{ ft}) \frac{1 \text{ m}}{3.28 \text{ ft}} = 0.0133 \text{ m}$$

$$\begin{aligned} X_1 &= \omega L_1 = 2\pi(60)2 \times 10^{-7} \ln\left(\frac{12.6}{0.149}\right) \frac{\Omega}{\text{m}} \times \frac{1000 \text{ m}}{1 \text{ km}} \\ &= 0.335 \Omega/\text{km} \end{aligned}$$

4.41

$$D_{eq} = \sqrt[3]{10 \times 10 \times 20} = 12.6 \text{ m}$$

$$\text{From Table A.4, } r = \frac{1.293}{2} \ln\left(\frac{0.0254 \text{ m}}{1 \text{ in}}\right) = 0.01642 \text{ m}$$

$$D_{sc} = \sqrt[3]{rd^2} = \sqrt[3]{0.01642(0.5)^2} = 0.16 \text{ m}$$

$$C_1 = \frac{2\pi\epsilon_0}{\ln\frac{D_{eq}}{D_{sc}}} = \frac{2\pi(8.854 \times 10^{-12})}{\ln\left(\frac{12.6}{0.16}\right)} = 1.275 \times 10^{-11} \text{ F/m}$$

$$\bar{Y}_1 = j\omega C_1 = j2\pi(60)1.275 \times 10^{-11}(1000) = j4.807 \times 10^{-6} \text{ S/km}$$

$$Q_1 = V_{LL}^2 Y_1 = (500)^2 4.807 \times 10^{-6} = 1.2 \text{ MVAR/km}$$

5.14

$$(a) \quad \bar{Z}_C = \sqrt{\frac{\bar{z}}{\bar{y}}} = \sqrt{\frac{0.03 + j0.35}{4.4 \times 10^{-6} \angle 90^\circ}} = 282.6 \angle -2.45^\circ \Omega$$

$$(b) \quad \bar{y}l = \sqrt{\bar{z}\bar{y}}(l) = \sqrt{(0.35128 \angle 85.101^\circ)(4.4 \times 10^{-6} \angle 90^\circ)}(500) \\ = 0.622 \angle 87.55^\circ = 0.02657 + j0.6210 \text{ pu}$$

5.38

From Problem 5.14

$$\bar{A} = 0.8794 \angle 0.66^\circ \text{ pu}; \quad A = 0.8794 \text{ and } \theta_A = 0.66^\circ$$

$$\bar{B} = \bar{Z}' = 134.8 \angle 85.3^\circ \Omega; \quad Z' = 134.8 \text{ and } \theta_Z = 85.3^\circ$$

$$P_{R \max} = \frac{500 \times 500}{134.8} - \frac{(0.8794)(500)^2}{134.8} \cos(85.3^\circ - 0.66^\circ) \\ = 1854.6 - 152.4 = 1702 \text{ MW (3}\phi\text{)}$$

For this loading at unity power factor,

$$I_R = \frac{P_{R \max}}{\sqrt{3} V_{RLL} (PF)} = \frac{1702}{\sqrt{3} (500)(1.0)} = 1.966 \text{ kA / Phase}$$

From Table A.4, the thermal limit for 3 ACSR 1113 kcmil conductors is $3 \times 1.11 = 3.33$ kA/p phase. The current 1.966 kA corresponding to the theoretical steady-state stability limit is well below the thermal limit of 3.33 kA.

5.41

$$(a) \quad \bar{Z} = \bar{z}l = (0.088 + j0.465)100 = 8.8 + j46.5 \Omega$$

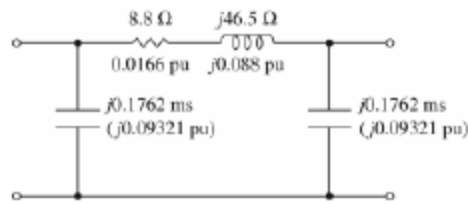
$$\frac{\bar{Y}}{2} = \frac{\bar{y}l}{2} = (j3.524 \times 10^{-6})100/2 = j0.1762 \text{ mS}$$

$$Z_{base} = V_{L, base}^2 / S_{3\phi, base} = \frac{(230)^2}{100} = 529 \Omega$$

$$\therefore \bar{Z} = (8.8 + j46.5) / 529 = 0.0166 + j0.088 \text{ pu}$$

$$\frac{\bar{Y}}{2} = j0.1762 / (1/0.529) = j0.09321 \text{ pu}$$

The nominal π circuit for the medium line is shown below:



$$(b) \quad S_{3\phi, rated} = V_{L, rated} I_{L, rated} \sqrt{3} = 230(0.9)\sqrt{3} = 358.5 \text{ MVA}$$