

Class 19: AC Problems

Problem 1. A communication channel receives a voltage waveform that consists of two frequencies: the audio signal at about 400 Hz and a noise signal at about 10 kHz. After amplification, the RMS magnitude of both of these waveforms is about 5 V. The speaker acts like a 3 Ohm resistor. In order to filter out the noise, a 0.1 mH inductor is placed in series with the speaker.

- a. Draw two versions of this circuit, one for each of the frequencies. The input can be modeled as an AC voltage source. Assume the phase angle for both is 0° .
- b. Calculate the impedances on each of the circuits at the different frequencies.
- c. Calculate the RMS current phasor at each of the frequencies.
- d. Calculate the voltage across the speaker (resistor) at each of the frequencies.
- e. Calculate the power absorbed by the speaker at each of the frequencies.
- f. What is the (1) unfiltered and (2) filtered signal-to-noise ratio, both in terms of voltage and power?
- g. What are the trade-offs in choosing the size of the inductor? What's the theoretical maximum signal-to-noise ratio? If you need at least 0.25 W on the speaker to be able to hear it, what is the highest signal-to-noise ratio you can get?

Problem 2. A factory is acting like a $250\ \Omega$ resistor in parallel with a $500\ \text{mH}$ inductor. A power distribution line supplying the factory from the substation can be modeled as a $65\ \text{mH}$ inductor. At the substation, the voltage is $12\angle 6.5^\circ\ \text{kV}$.

- a. Draw this circuit and find the impedance of the circuit elements. The substation can be modeled as a voltage source. The frequency is $60\ \text{Hz}$.
- b. What is the voltage at the factory?
- c. How much active and reactive power is the factory absorbing?
- d. What is the factory's power factor?
- e. If a $50\ \mu\text{F}$ capacitor is installed in parallel with the factory, how do the voltage and power factor change?
- f. What should the value of the capacitor be so that the power factor is 0.95 lagging?